

# Practical Secure Function Evaluation

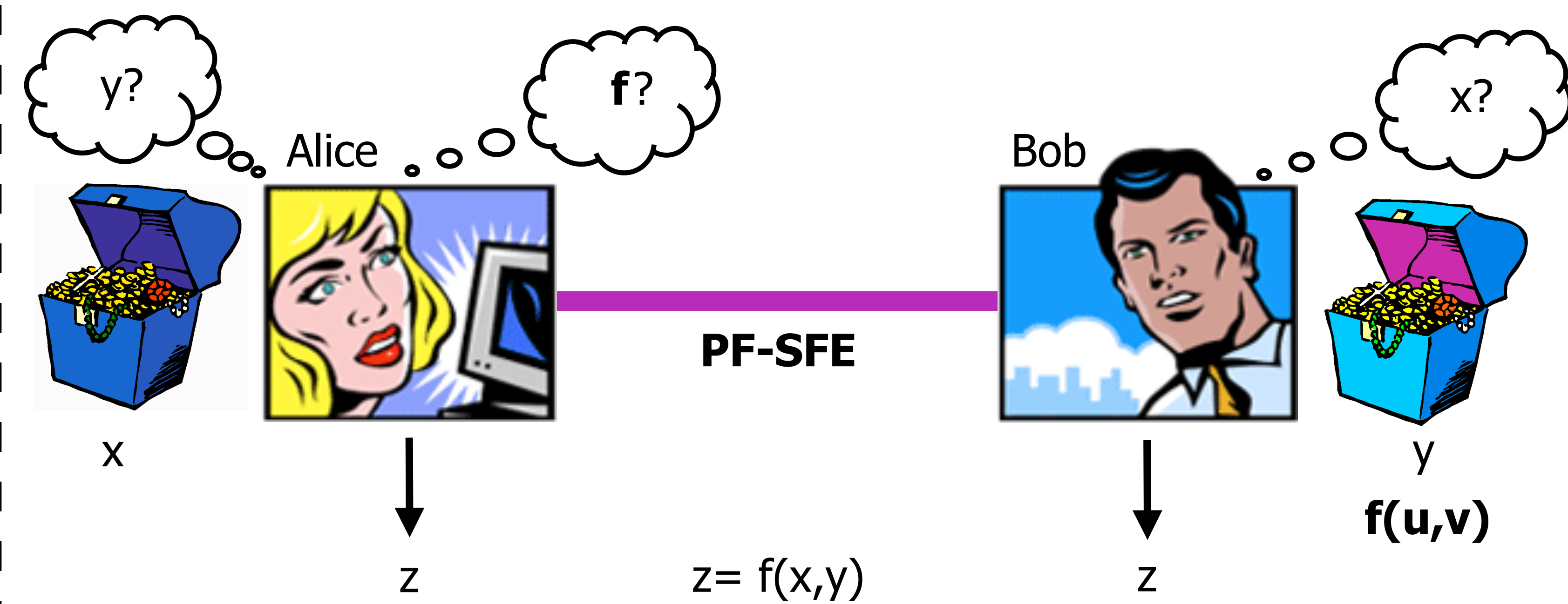
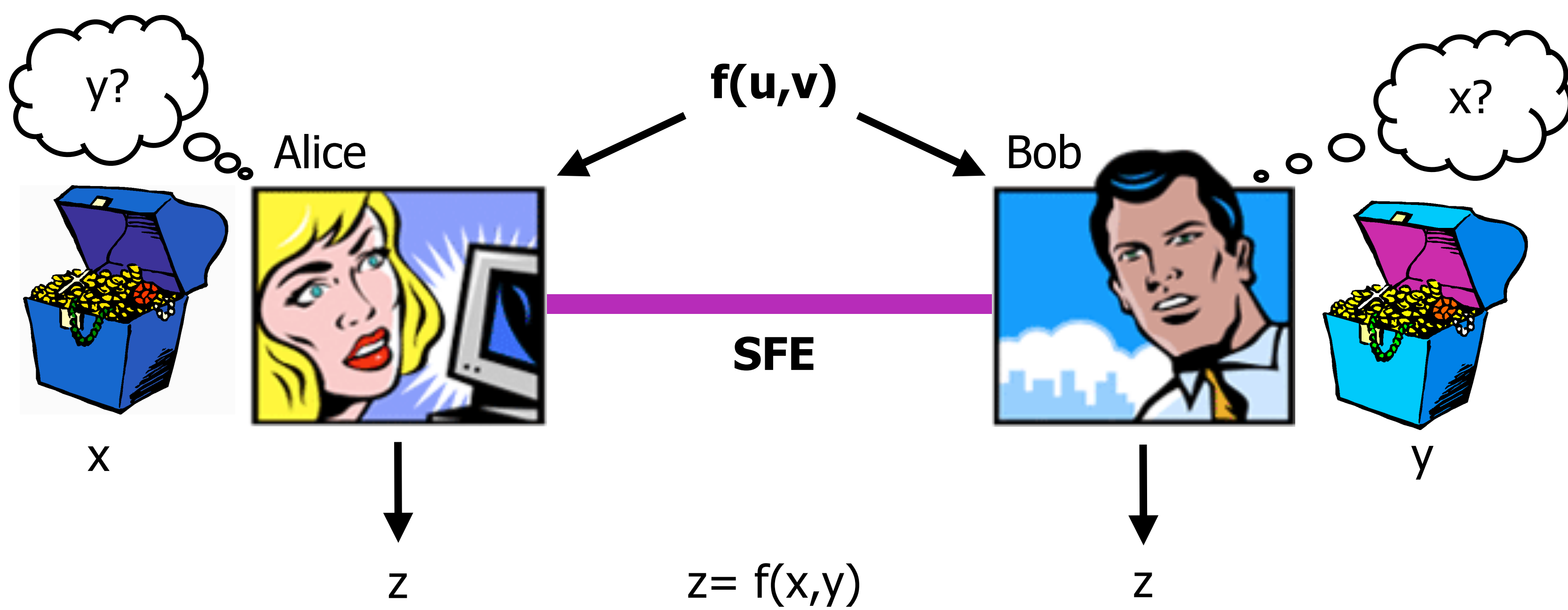
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**Secure Function Evaluation (SFE)** allows two parties Alice and Bob to securely evaluate a function  $f(u,v)$  on their private inputs  $x$  and  $y$ :

- each party learns the result  $z = f(x,y)$
- each party learns nothing about the other party's secret  $y$  resp.  $x$

**Secure Function Evaluation of Private Functions (PF-SFE)** - same as SFE with additionally  $f$  being private:

- $f$  is known by Bob only
- Alice learns nothing about  $f$  (besides size, #inputs and #outputs)



Practical Examples:

- Millionaires Problem (Maximum)
- Auctions
- Voting
- Keyed Database Search
- ...

Practical Examples:

- No-Fly-List Checking
- Privacy-Preserving Credit Report (or Medical History) Checking
- Mobile Code (executed in untrustworthy environment)
- Privacy-Preserving Database Querying (e.g. patent database)
- ...

## Contents and Contributions of this Thesis:

Summary and comparison of **known SFE protocols** with different representations of the boolean function  $f$  as boolean circuit or ordered binary decision diagram (OBDD).

Extension of OBDD-based SFE protocol [KJGB06] (secure in semi-honest model) to malicious model and **OBDD-based PF-SFE protocol** with small overhead.

PF-SFE can be reduced to SFE of a Universal Circuit (UC) that can be programmed to compute any function  $f$  of size  $k$  gates. Our **practical UC construction\*** [KS08] is up to 50% smaller than the best UC of Valiant [Val76] when used in today's PF-SFE.

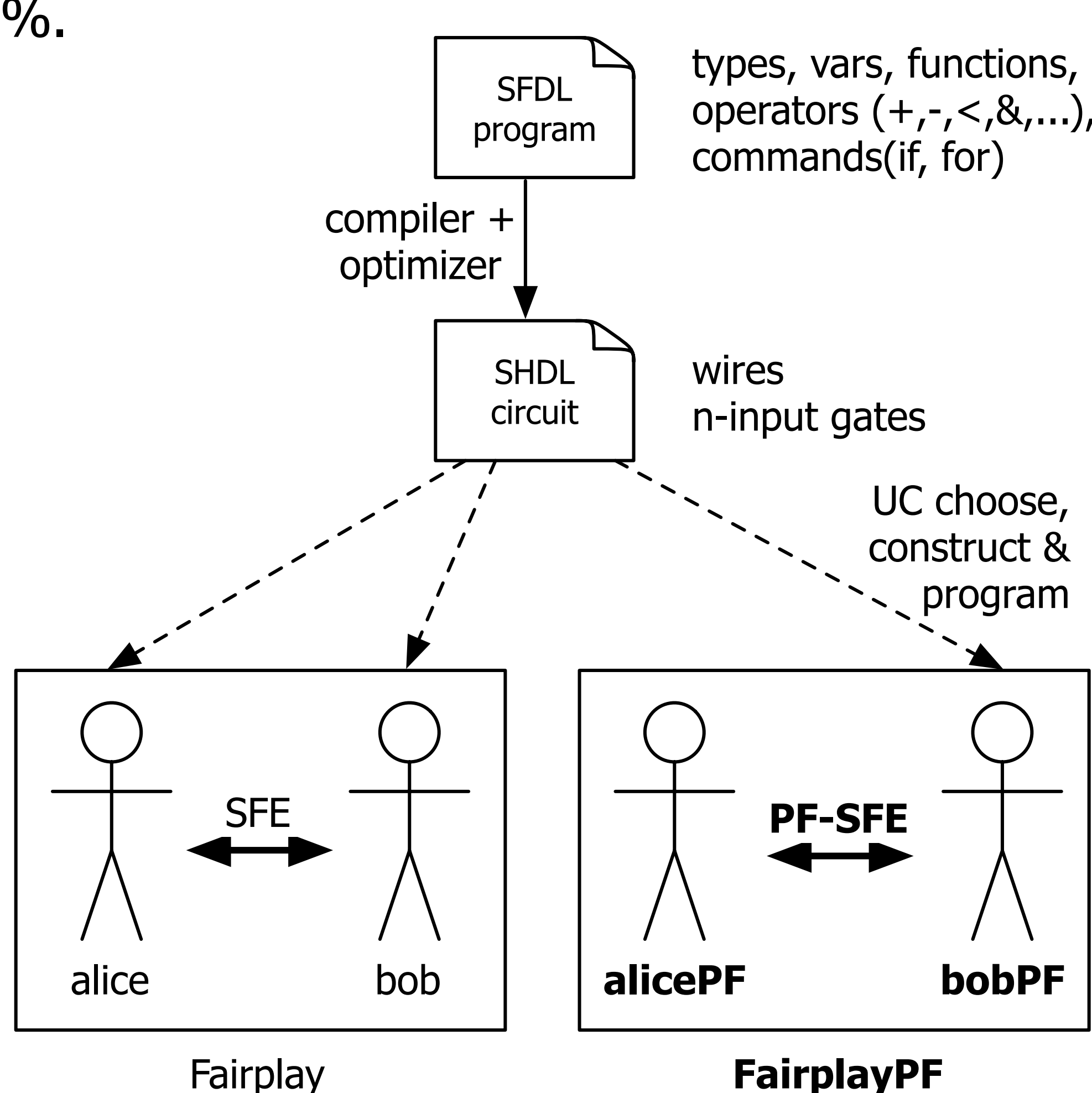
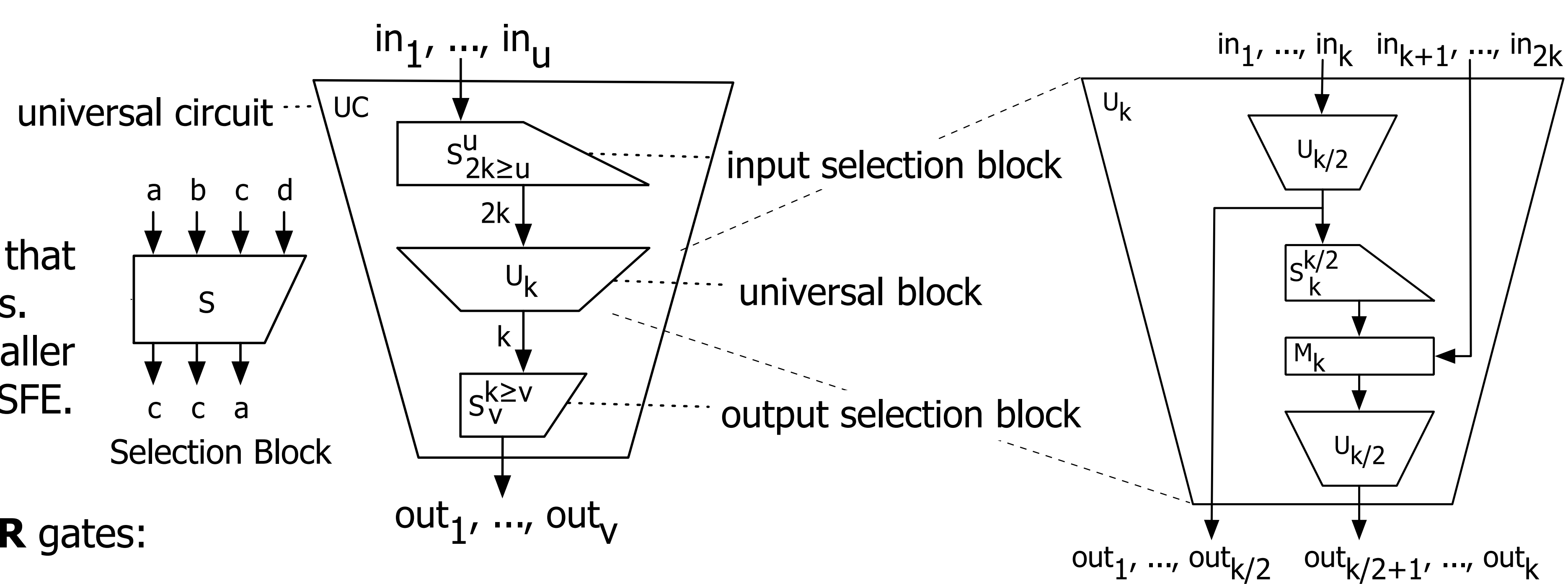
Our **improved SFE protocol\*** allows **free** evaluation of **XOR** gates:

- Based on SFE protocols Fairplay [MNPS04] & GESS [Kol05].
- Improves many important functions (e.g. addition, equality test) to 50%.
- UC-based PF-SFE protocols can be improved to even 25%.

Implementation of **FairplayPF**, an extension of the well-known Fairplay SFE system for practical PF-SFE.

<http://thomaschneider.de/FairplayPF>

Function Represent.	SFE Protocol	Proof of Security			Evaluation Speed (Encryption Scheme)
		semi-honest	malicious	RO	
Circuit	Yao [Yao86]	X			slow ( $E_{spec}$ )
	Fairplay [MNPS04]	X	X	X	medium (H)
	GESS [Kol05]	X		X	very fast (XOR)
	improved SFE	X	X	X	medium/very fast (H/XOR)
OBDD	OBDD SFE [KJGB06]	X			slow ( $E_{spec}$ )
	improved OBDD SFE	X	X		fast (E)



### Bibliography

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