FAPRIL: Towards Faster Privacy-Preserving Fingerprint-Based Localization

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Abstract: Fingerprinting is a commonly used technique to provide accurate localization for indoor areas, where global navigation satellite systems, such as GPS and Galileo, cannot function or are not precise enough. Although fingerprint-based indoor localization has gained wide popularity, existing solutions that preserve privacy either rely on non-colluding servers or have high communication which hinder deployment.

In this work we present FAPRIL, a privacy-preserving indoor localization scheme, which takes advantage of the latest secure two-party computation protocol improvements. We can split our scheme into two parts: an input independent setup phase and an online phase. We concentrate on optimizing the online phase for mobile clients who run on a mobile data plan and observe that recurring operands allow to optimize the total communication overhead even further. Our observation can be generalized, e.g., to improve multiplication of Arithmetic secret shared matrices. We implement FAPRIL on mobile devices and our benchmarks over a simulated LTE network show that the online phase of a private localization takes under 0.15 seconds with less than 0.20 megabytes of communication even for large buildings. The setup phase, which can be pre-computed, depends heavily on the setting but stays in the range 0.28 – 4.14 seconds and 0.69 – 16.00 megabytes per localization query. The round complexity of FAPRIL is constant for both phases.

1 INTRODUCTION

Localization is conventionally based on Global Navigation Satellite Systems (GNSSs), such as GPS or Galileo. However, the downside of GNSSs is their decreased accuracy when the satellite signals are blocked by obstacles. This is particularly a problem for indoor areas, such as shopping malls or airports. Hence new techniques have been developed and deployed specifically for Indoor Localization (IL), see (Lan-glois et al., 2017; Yassin et al., 2017) for surveys. The IL techniques are commonly based on using Wi-Fi (Ladd et al., 2005; Haeberlen et al., 2004), cellular (Talvitie and Lohan, 2013), RFID (Chawla et al., 2013), Bluetooth (Chen et al., 2011), or Zigbee (Noh et al., 2008) signals. Localization using Wi-Fi signals is particularly tempting for public buildings having a Wi-Fi Access Point (AP) infrastructure already in place. Besides this, the increase in the number of smartphones and other mobile devices capable of measuring Received Signal Strengths (RSSs) from Wi-Fi APs makes it easy for people to use these techniques without having to buy an extra device. In the future, even cellular signals could become interesting source of RSSs via dense 5G networks (Hakkarainen et al., 2015), providing accurate localization for both indoors and outdoors.

Relatively cheap and accurate IL has gained interest from different Service Providers (SPs) resulting in an increase in the number of Location-Based Services (LBSs) developed for indoor areas such as museums, shopping malls, airports, exhibition centers, hospitals, and university campuses (see, e.g., (Guan et al., 2017; He et al., 2017)). The most interesting services include indoor navigation, routing to a given destination, finding nearby friends, and targeted advertising (see, e.g., (Alletto et al., 2015; Li et al., 2017)). The recent study in (Barsocchi et al., 2021) also discusses the potentials of using different IL technologies for measuring the distance among the users and enhancing...
social distancing effectively in indoor environments.

However, location information is highly privacy sensitive and could be exploited to predict persons’ future movements and even identify them (Bellovin et al., 2013). In addition, SPs might have to comply with privacy laws and regulations, such as the EU General Data Protection Regulation (GDPR), forcing them to use privacy-preserving solutions. The privacy aspects of LBSs are well studied (see, e.g., (Stirbys et al., 2017; Hallgren et al., 2017; Järvinen et al., 2018)). However, the studies mainly focus on how the location information is handled in the service itself after the client has already performed the actual localization. In our paper, the focus is on the privacy concerns of the actual location retrieval, which is a natural prerequisite for privacy-preserving LBSs.

Whereas GNSS based localization is inherently privacy-preserving (see (Chen et al., 2017; Lohan et al., 2017a)), for IL techniques privacy is harder to achieve. In our paper, we focus on fingerprint-based localization, which is the most prominent IL technique used with Wi-Fi APs (see, e.g., (Capkun et al., 2011; Guan et al., 2017; Yin et al., 2017)). Fingerprint-based localization relies on a pre-constructed database, which contains so called fingerprints. Each fingerprint is basically a vector, where each element is a RSS value from a different source such as a Wi-Fi AP. The fingerprints are pre-measured around the building or area at various known locations called reference points. In the location retrieval step, the user measures its own fingerprint, which is then compared to the fingerprints in the database. In a typical scenario, the Service Provider (SP) holds the database on a server that compares with the user’s fingerprint. However, this leaks the user’s location to the server, and thus to the SP.

A naive solution against leaking the user’s location would be to send the whole database to the user’s device. This maintains privacy for the user, since now the location retrieval includes only local computations. However, it violates the privacy of the server and SP by leaking the database content to the users, and thus releasing the database practically to the public. The reasons why the database should be kept secret from the public are already discussed in several related works (see §1.1). The database has high value, since constructing it is laborious manual work. In practice, SPs still tend to have the power and control over the users on what information is leaked. Since the database is basically the only valuable asset for the SP in fingerprint-based localization and might even leak delicate details of the building construction (e.g., suspiciously thick or thin walls), we expect that the SPs tend to sacrifice users’ privacy unless better solutions are available.

Privacy-Preserving Indoor Localization (PPIL) tries to solve the privacy issues regarding both the users’ location information and the database. However, the previously proposed PPIL schemes suffer from drawbacks such as low performance and high data transfer rates, which discourage an actual deployment.

### 1.1 Related Work

One of the earliest fingerprint-based PPIL scheme proposals in the literature for the client-server setting without using trusted third parties was PriWFL (Li et al., 2014) presented in INFOCOM’14. The scheme uses Paillier encryption (Paillier, 1999) to preserve clients’ privacy but tries to hide the database information with an ad hoc masking technique, which was found later insecure (Yang and Järvinen, 2018).

The authors of (Shu et al., 2014) proposed a PPIL scheme using Paillier encryption and Oblivious Transfer (OT). The scheme relies on other mobile devices with known location, which is a major drawback in practice. Additionally, computationally heavy operations are performed on the client’s mobile device, which leads to performance and battery-power problems.

The authors of (Ziegeldorf et al., 2014) based their PPIL scheme on the Hidden Markov Model and use Homomorphic Encryption (HE) for the computations. The performance of their solution is poor, since the location retrieval takes around 10 seconds even in a relatively small building when using powerful servers and a fast LAN network.

The authors of (Konstantinidis et al., 2016) proposed a PPIL scheme based on k-anonymity. The downside of their scheme is that the privacy guarantees become weaker if auxiliary information, such as the building map, is provided to the adversary. On the other hand, if the security parameter sizes are increased, the location accuracy decreases and the scheme becomes impractical.

Järvinen et al. proposed PILOT (Järvinen et al., 2019), which was the first efficient solution for PPIL. PILOT uses well known Secure Two-Party Computation (STPC) techniques and outsources the most involving computations to two semi-trusted servers in order to achieve practical performance. Their work includes benchmarks with various combinations of STPC techniques. The outsourcing setting assumes that the two servers are non-colluding, which are hard to find (e.g., the owner of the building and the mobile network operator). Their underlying protocols are suitable also for the client-server setting, and so we consider (Järvinen et al., 2019) as an excellent basis for developing more efficient PPIL schemes. The main disadvantage of PILOT is the large communica-
We provide the following contributions in our paper: we achieve online times of only $0$ where parties have limited data plans. In our work, we present techniques, which reduce the total communication by factor $16 \times$ with a very efficient online phase. The authors of (Nieminen and Järvinen, 2020) proposed a PPIL scheme in the client-server setting using Paillier encryption and Garbled Circuits (GCs). We call their solution NJ in our paper. NJ does not rely on trusted third parties or outsourcing, but involves relatively expensive operations leading to online times of $1.55 - 8.46$ seconds. On top of this, their scheme requires computationally heavy pre-computations in the setup phase, which take $2.45 - 12.23$ seconds for each localization query. Compared to PILOT (Järvinen et al., 2019), NJ achieves better total communication overheads making it suitable for the mobile client setting. In contrast to NJ (Nieminen and Järvinen, 2020), we achieve online times of only $0.15$ seconds and need only $0.28 - 4.14$ seconds for the setup phase without increasing the communication overhead.

### 1.2 Our Contributions

We provide the following contributions in our paper:

- **We design and implement FAPRIL**, a fingerprint-based client-server Privacy-Preserving Indoor Localization (PPIL) scheme using STPC techniques that enables fast localization for users without leaking the actual location to third parties. Additionally, FAPRIL provides privacy to SPs keeping their database private. We show that FAPRIL achieves practical run-times even in large settings, and when the client is using a regular smartphone. Compared to today’s best known client-server PPIL scheme (Nieminen and Järvinen, 2020), our protocol avoids expensive additively homomorphic encryption and has a $8 \times$ faster setup time, $27 \times$ faster online time, $6 \times$ less online communication, and only $1.11 \times$ more setup communication (cf. Tab. 3). Compared to PILOT (Järvinen et al., 2019), we achieve $16 \times$ less communication in the setup phase, and $20 \times$ less communication in the online phase.

- **Our main goal is to optimize the input-dependent online phase which is run over a mobile data-plan in PPIL**. For this, we use the state-of-the-art secure two-party computation protocols from ABY2.0 (Patra et al., 2021) that allow scalar products with online communication independent of the dimension of the vector. This yields an order of magnitude better online communication than the ABY (Demmler et al., 2015)-based PPIL protocols of PILOT (Järvinen et al., 2019) (see §5.3).

### 2 Preliminaries

In this section, we describe the general fingerprint-based localization technique commonly used for Indoor Localization (IL) with different distance metrics. Thereafter, we summarize the relevant Secure Two-Party Computation (STPC) techniques used in FAPRIL.

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1. We use an Arithmetic sharing based approach, since it outperforms solutions relying on public key cryptography such as (Wang et al., 2017; Mishra et al., 2021).

2. We use a Garbled Circuit (GC) based approach to preserve accuracy. Approximate and non-constant round $k$-Nearest Neighbor Algorithms (kNNs) have been studied, e.g., in (Shaul et al., 2020; Chen et al., 2020; Zubir and Sirdey, 2021; Mohassel et al., 2020).
2.1 Fingerprint-Based Localization

Indoor areas, such as airports and shopping malls, need non-Global Navigation Satellite System (GNSS) based techniques for accurate localization, since ceilings or other obstacles often block the satellite signals. A common solution for Indoor Localization (IL) is fingerprint-based localization (see, e.g., (Bahl and Padmanabhan, 2000; Liu et al., 2007)), which requires the Service Provider (SP) to pre-construct a database holding a set of pre-measured fingerprints. The fingerprints contain Received Signal Strengths (RSSs) measured from different Access Points (APs) (e.g., Wi-Fi). The set of used APs is fixed and public for the localization setup and can be based on, e.g., MAC addresses. We assume to have $N$ APs and the pre-measured fingerprints are measured from $M$ reference points around the area or building. The database is written as $\mathcal{D} = \{V_1, \ldots, V_M\}$, where $V_i$ denotes the pre-measured fingerprint from the $i$-th reference point (denoted as $\chi_i$). A pre-measured fingerprint is written as $V_i = \{v_{i,1}, \ldots, v_{i,N}\}$, where $v_{i,j}$ denotes the RSS at $\chi_i$ from the $j$-th AP. After the construction, $\mathcal{D}$ is normally placed on a server $\delta$ offering the localization service to users, a.k.a. clients.

Location retrieval of a client $c$ goes as follows: $c$ measures its own fingerprint $F = \{f_1, \ldots, f_N\}$ and compares $F$ to each $V_i$, $i \in \{1, \ldots, M\}$ using a specific distance metric (see §2.1.1). A small distance $d_i$ between $F$ and $V_i$ means that the fingerprints are similar implying that $c$ is likely to be near $\chi_i$. For many settings, it is beneficial (for better accuracy) to take the average location of multiple reference points $\chi_i$ corresponding to $V_i$ for which the distance to $F$ is the smallest. These points can be determined by the $k$-Nearest Neighbor Algorithm (kNN), which here outputs a set of nearest reference points $\{\chi_{i_1}, \ldots, \chi_{i_k}\}$. The final location output to $c$ is normally the centroid of the $k$ reference points $\{\chi_{i_1}, \ldots, \chi_{i_k}\}$.  

### 2.1.1 Distance Metrics

In fingerprint-based localization, the server $S$ computes distances $d_i$ between $F$ and $V_i$ for $i \in \{1, \ldots, M\}$. Different distance metrics for fingerprint-based IL have been studied before (see, e.g., (Richter et al., 2018; Järvinen et al., 2019)). To optimize performance, we focus on the squared Euclidean distance calculated as shown in Eq. (1).

$$d_i^F = \sum_{j=1}^{N} (f_j - v_{i,j})^2$$  \hspace{1cm} (1)
2.2.1 Arithmetic and Delta Sharing

The Arithmetic sharing protocol, due to GMW (Goldreich et al., 1987), enables two parties $P_0$ and $P_1$ to evaluate a function on secret shared values. The function is expressed as an Arithmetic circuit consisting of addition and multiplication gates and the operations are performed in the ring $\mathbb{Z}_{2^f}$. We denote the Arithmetic sharing of $x$ with $[x]$ and the random shares with $[x]_0, [x]_1$ respectively for $P_0, P_1$. In order for $P_i, i \in \{0, 1\}$ to secret share $x \in \mathbb{Z}_{2^f}$, $P_i$ chooses a random value $r \in \mathbb{Z}_{2^f}$ and sets $[x]_{i} = x - r \pmod{2^f}$ and $[x]_{1-i} = r$. Now $P_i$ keeps $[x]_{i}$ and sends $[x]_{1-i}$ to $P_{1-i}$. It is easy to see that $[x]_0 + [x]_1 = x \pmod{2^f}$.

The authors of (Patra et al., 2021) proposed an optimized variant of the general Arithmetic sharing protocol, which we refer to as Delta sharing protocol from now on. With their technique, the online communication per multiplication gate is reduced in half. More importantly for us, they present an efficient protocol for scalar product, which achieves an online communication complexity independent of the vector dimension. We denote the Delta sharing of $x$ with $\langle x \rangle$ and the random shares with $\langle x \rangle_i$ for $P_i, i \in \{0, 1\}$. Addition gates are local computations. Multiplication requires an interactive protocol and Multiplication Triples (MTs). In our work, we generate the MTs via the Correlated Oblivious Transfer (C-OT) protocol of (Asharov et al., 2013). We refer the reader to (Patra et al., 2021) for the details on the Delta sharing semantics.

2.2.2 Yao Sharing

Yao sharing is based on Yao’s Garbled Circuits (GCs) (Yao, 1986) and enables two parties to securely evaluate a function expressed as a Boolean circuit. The basic idea of GCs is the following: one of the parties, called the garbler, assigns two randomly chosen symmetric keys to all wires called garbled values. For all gates, the garbler uses the input keys to encrypt the corresponding output key. Next, the garbler sends the encrypted gates (called garbled circuit) to the other party, typically referred to as the evaluator, along with the symmetric keys corresponding to its input bits. The evaluator obtains the symmetric keys corresponding to its input bits via an Oblivious Transfer (OT) protocol implemented efficiently using OT extension (Ishai et al., 2003; Asharov et al., 2013). Finally, the evaluator evaluates the garbled circuit by decrypting the garbled gates obtaining the garbled output values. In order to reveal the actual output values to the evaluator, the garbler provides the evaluator with information to decode the output wires.

Over the years, several optimization techniques for GCs have been introduced. These include point-and-permute (Beaver et al., 1990), free-XOR (Kolesnikov and Schneider, 2008), fixed-key AES garbling (Bellare et al., 2013), and half-gates (Zahur et al., 2015). Recently, Rosulek and Roy (Rosulek and Roy, 2021) introduced a new GC optimization, which defeats half-gates (Zahur et al., 2015). However, we exclude this technique from our implementation of FAPRIL, mainly in order to have a fair comparison with the related works, which can also benefit from this optimization.

2.2.3 From Arithmetic/Delta to Yao Sharing

The conversion from Arithmetic shares to Yao shares is described in (Demmler et al., 2015). The conversion for the Delta sharing protocol is described in (Patra et al., 2021), but follows the same idea: the Boolean circuit for Yao’s GCs begins by adding the Arithmetic shared values from both parties. With Delta sharing the C-OT step can be performed in the setup phase in contrast to Arithmetic sharing, where this is in the online phase.

3 SYSTEM DETAILS

In this section, we give an overview of FAPRIL, our PPIL scheme in the client-server setting based on mixed-protocol Secure Two-Party Computation (STPC), namely Delta and Yao sharing (see §2.2). A high-level overview is given in §3.1 and a more detailed description follows in §3.2 containing also the complexity analysis. Finally, the security aspects are discussed in §3.3.

3.1 Overview

Here we give a high-level overview of FAPRIL, which uses Delta and Yao sharing to provide privacy-preserving fingerprint-based localization. Our scheme follows the idea from (Järvinen et al., 2019), where the most cost efficient localization was achieved using the combination of Arithmetic sharing, which we improve to Delta sharing, and Yao sharing. Additionally, we select the squared Euclidean distance to be our distance metric (see §2.1.1), since it gives arguably the best cost-accuracy ratio for Privacy-Preserving Indoor Localization (PPIL), see (Järvinen et al., 2019). We denote the number of used Access Points (APs) with $N$ and the number of reference points with $M$ (see §2.1).

After the client $c$ has measured its fingerprint $F$, it Delta shares $F$ with the server $S$ such that $\langle F \rangle = \{ \langle f_1 \rangle, \ldots, \langle f_N \rangle \}$. Additionally, $c$ Delta shares $\sum_{j=1}^{N} f_j^2$ with $S$. Similarly, $S$ Delta shares
each pre-measured fingerprint $V_i$ along with $\sum_{i=1}^{M} v_{i,j}$, $i \in \{1, \ldots, M\}$ from the database $D$. After the sharing, both parties have obtained their respective shares $\{F\}, \{\sum_{i=1}^{M} f_{i,j}\}$ and $\{V_i\}, \{\sum_{i=1}^{M} v_{i,j}\}$, where $\langle V_i \rangle = \{\langle v_{i,1} \rangle, \ldots, \langle v_{i,N} \rangle\}$.

Next, both parties compute the squared Euclidean distances using their respective shares using Eq. (2), which is directly derived from Eq. (1).

$$
\langle d_{i} \rangle = \left\langle \sum_{j=1}^{N} f_{i,j}^2 \right\rangle + \left\langle \sum_{j=1}^{N} v_{i,j}^2 \right\rangle - 2 \sum_{j=1}^{N} \langle f_{i,j} \rangle \cdot \langle v_{i,j} \rangle
$$

Eq. (2) requires $N$ multiplications, and thus the total number of multiplications to obtain all $\{\langle d_{i} \rangle\}_{i=1}^{M}$ is $N \cdot M$.

We note that $\sum_{j=1}^{N} \langle f_{i,j} \rangle \cdot \langle v_{i,j} \rangle$ is a scalar product between $\langle F \rangle$ and $\langle V_i \rangle$, and thus we can compute it with the optimized Delta sharing scalar product of (Patra et al., 2021). More generally, we can reduce the problem of computing $\sum_{j=1}^{N} \langle f_{i,j} \rangle \cdot \langle v_{i,j} \rangle$ down to a vector-matrix multiplication (plus cheap addition operations with the shares afterwards). More formally, we transform the fingerprint $F$ to a vector of length $N$ and the database $D$ into a $M \times N$ matrix. The Delta shared versions are as follows:

$$
\langle F^N \rangle = \begin{bmatrix} \langle f_1 \rangle & \langle f_2 \rangle & \cdots & \langle f_N \rangle \end{bmatrix},
$$

$$
\langle D^{M \times N} \rangle = \begin{bmatrix} \langle v_{1,1} \rangle & \langle v_{1,2} \rangle & \cdots & \langle v_{1,N} \rangle \\
\langle v_{2,1} \rangle & \langle v_{2,2} \rangle & \cdots & \langle v_{2,N} \rangle \\
\vdots & \vdots & \ddots & \vdots \\
\langle v_{M,1} \rangle & \langle v_{M,2} \rangle & \cdots & \langle v_{M,N} \rangle \end{bmatrix}.
$$

The distances are obtained by first computing the vector-matrix multiplication $\langle F^N \rangle \cdot \langle D^{M \times N} \rangle^T$, where $T$ is the transpose operator. The result is a vector of length $M$ containing $\sum_{j=1}^{N} \langle f_{i,j} \rangle \cdot \langle v_{i,j} \rangle^M$. These values are used with Eq. (2) requiring a total of 3 additions. Note that all the operations are in $Z_{2^\ell}$, where $\ell$ is the bit-length of $d_i$.

In the last step of FAPRIL, the client $C$ uses the $k$ indices to obtain the $k$ reference points $\{\chi_1, \ldots, \chi_k\}$. Here we assume, similarly to (Nieminen and Järvinen, 2020), that the server $S$ has published the set of reference points $\{\chi_{i}\}_{i=1}^{M}$ to the public.

### 3.2 Details and Complexity

We move on to a more precise description of the steps of FAPRIL and the complexity of these steps. Certain parameters, such as the list of Access Points (APs) and the security parameter $\kappa$, are negotiated between the client $C$ and the server $S$ in a one-time initialization step. The resulting overhead is not very interesting, since it does not accumulate over time. Moreover, the parameters can be included in the client application as hard coded values.

FAPRIL uses the Oblivious Transfer (OT) extension protocol of (Asharov et al., 2013), which requires so called base OT in the initialization step. In fact, our implementation of FAPRIL (see §5) uses two different OT flavors and we need to run two different base OT steps. However, the steps are independent of $M$ and $N$, and require under 1 second and 30 kilobytes of communication in total. They can also be reused for multiple protocol runs between $C$ and $S$. We conclude that these overheads are negligible.

We separate FAPRIL into two phases, namely setup and online phase. The setup phase is independent of $C$‘s fingerprint $F$ and can be computed in advance, e.g., multiple times overnight using a relatively fast Wi-Fi connection. The online phase depends on $F$ and must be performed only after $C$ has measured the Received Signal Strengths (RSSs).

#### 3.2.1 Setup Phase

In the setup phase, we generate the Multiplication Triples (MTs) for the multiplication operations with the Delta shares as shown in Eq. (2). MTs can be generated in various ways using OT or HE (Rathee et al., 2019). Due to the necessity to implement on a mobile device, we choose to use the OT-based multiplication protocol by Gilboa (Gilboa, 1999) with Correlated Oblivious Transfer (C-OT) as in (Demmler et al., 2015). With the optimization technique from (Demmler et al., 2015), the total communication needed to construct an $\ell$-bit MT is $2\ell (\kappa + (\ell + 1)/2)$ bits, where $\kappa$ is the security parameter. We set $\kappa = 128$ for FAPRIL. The multiplications are performed in $Z_{2^\ell}$, where $\ell$ is the bit-length of $d_i$, $i \in \{1, \ldots, M\}$. We can calculate $\ell$ with Eq. (3), where $\ell_{RSS}$ is the bit-length...
of \( f \) and \( v \), i.e., \( \ell_{\text{RSS}} \) follows from the quantization of RSSs.

\[
\ell = \left\lfloor \log_2 \left( (2^{\ell_{\text{RSS}}} - 1)^2 \cdot N \right) \right\rfloor \tag{3}
\]

For FAPRIL, we fix \( \ell_{\text{RSS}} = 4 \) as it was shown to provide the same level of accuracy as longer bit-lengths (Richter et al., 2018) (see also §2.1.2). We simplify Eq. (3) accordingly to get Eq. (4).

\[
\ell = \left\lfloor \log_2 225N \right\rfloor \approx 8 + \left\lfloor \log_2 N \right\rfloor \tag{4}
\]

As stated earlier, the total number of multiplications needed is \( N \cdot M \). Hence, we need a total of \( N \cdot M \cdot 2/(\kappa + (\ell + 1)/2) \) bits of communication. If \( N = 241 \) and \( M = 505 \), we have \( \ell = 16 \) and the communication needed for the MT generation is 63.4 megabytes. However, later in §4 we propose an optimization technique to reduce this communication down to 4.2 megabytes making FAPRIL more practical for smartphone clients with limited mobile data plans. Each MT generation with C-OTs requires 6\( b \) symmetric cryptographic operations, so \( N \cdot M \cdot 6\ell \) in total.

The client \( C \) needs to obtain its garbled input values from the server \( S \) for the conversion step from Delta to Yao sharing. This is normally performed with a C-OT protocol in order to comply with the free-XOR GC optimization technique (Kolesnikov and Schneider, 2008). In general, this step should be in the online phase, since the inputs (the Delta shares of distances) depend on \( C \)'s input. However, due to the nature of Delta shares we can move this step in the setup phase (as was already pointed out in (Patra et al., 2021)). The required communication for this step is \( M \cdot 2/(2\ell + \lfloor \log_2 M \rfloor) \) AND gates. This gives us the total number of AND gates, namely \#AND = \( M \cdot (2\ell + \lfloor \log_2 M \rfloor + \ell) \). The required communication is \( 2\kappa \cdot \#\text{AND} \) bits and the garbler needs to perform \( 4 \cdot \#\text{AND} \) fixed-key AES operations. With \( N = 241, M = 505 \), and \( \kappa = 3 \) we get \#AND = 70195, which translates to 2.1 megabytes of communication.

Finally, we note that the MT generation is independent of the other steps and can be performed in parallel in order to reduce the total run-time. The total theoretical setup communication with state-of-the-art optimizations (including (Rosulek and Roy, 2021) and §4) is 6.0 megabytes, when \( N = 241, M = 505, k = 3 \).

### 3.2.2 Online Phase

In the online phase, the client \( C \) measures its fingerprint \( F \) and runs a private localization query with the server \( S \). The first step for \( C \) is to Delta share \( F \) and \( \sum_{j=1}^{N} f_j \) with \( S \) as explained in §3.1. This requires communication of \( (N + 1) \cdot \ell \) bits from \( C \) to \( S \) and only simple computations. For \( N = 241, M = 505 \), this step requires 0.5 kilobytes of communication.

Then both parties compute the distances \( \{ d_i \}_{i=1}^{M} \) (in parallel) following Eq. (2) and using the efficient scalar product from (Patra et al., 2021). As stated in §2.2.1, the communication is independent of the vector length (here \( N \)) and the total communication is \( M \cdot 2\ell \) requiring only one round of communication. This step also requires only simple computations when MTs are pre-computed in the setup phase. For \( N = 241, M = 505 \), this step requires 2.0 kilobytes of communication.

Next, \( S \) sends its garbled input values corresponding to its shares \( \{ d_i \}_{i=1}^{M} \) to \( C \). This step does not require any computations and the size of the garbled values is \( \kappa \cdot M \cdot \ell \). For \( N = 241, M = 505 \), this step requires 126.3 kilobytes of communication.

In the last step, \( C \) evaluates the garbled circuit and obtains \( k \) indices. The evaluation requires \( 2 \cdot \#\text{AND} \) fixed-key AES operations with (Zahur et al., 2015). This step does not require communication. The permutation bits (Beaver et al., 1990) of the output garbled values can be used to reveal the actual output values. Alternatively, \( S \) can send the signal bits for all output wires, requiring \( k \cdot \log_2 M \) bits of communication.

For \( M = 505, k = 3 \), this step requires 27 bits of communication.

Finally, we conclude that the communication complexity of the online phase is orders of magnitude smaller than that of the setup phase. The total theoretical online communication is 128.8 kilobytes, when \( N = 241, M = 505, k = 3 \). FAPRIL shifts very efficiently most of the computation and communication in the setup phase, making it very attractive for applications which require fast location retrievals but allow pre-computations, e.g., overnight.

### 3.3 Security and Privacy Discussion

In this section, we give a brief security analysis of FAPRIL in §3.3.1. Furthermore, we discuss different privacy aspects regarding the reference points in §3.3.2.

FAPRIL is secure in the semi-honest adversary...
model, a.k.a. “honest-but-curious” adversary model, which assumes that both parties follow the protocol specification, but try to learn additional information from the transcript, i.e., from the received messages. Most of the related work on Privacy-Preserving Indoor Localization (PPIL) relies on the same semi-honest adversary model and it is widely used in many other applications including Privacy-Preserving Machine Learning (PPML).

3.3.1 Security Analysis

FAPRIL uses well-known Secure Two-Party Computation (STPC) techniques in a rigorous way. Technically, FAPRIL can be divided into three parts, namely computation of an Arithmetic circuit in Delta sharing, conversion from Delta to Yao sharing, and computation of a Boolean circuit in Yao sharing (see §2.2). The latter two are based on Yao’s Garbled Circuit (GC) protocol, which was proven secure for semi-honest adversaries in (Lindell and Pinkas, 2009). For the security proof of the other parts, we refer the reader to the full version of (Patra et al., 2021). In summary, the security follows from the security assumptions of the underlying primitives, which for FAPRIL is Oblivious Transfer (OT), which was proven secure in (Asharov et al., 2013). The security of FAPRIL persists for multiple sequential queries. However, auxiliary information, such as how frequently the client makes queries is always “leaked” outside the protocol execution to the Service Provider (SP).

It is also important that the client communicates with the servers over the mobile network but not via Wi-Fi APs, which are controlled by the SP. This would leak the client’s location, since the SP can see from which AP the client communicates and can use triangulation to determine the location. However, this is not related to the RSS values used in FAPRIL and is not a leakage of our scheme.

In conclusion, FAPRIL utilizes all the primitives as a black box, from which the security guarantees follow automatically. FAPRIL guarantees passive security, i.e., security against semi-honest adversaries. We note that since our scheme is based on STPC techniques which also have variants to withstand stronger security models, the security guarantees of FAPRIL can be enhanced using standard methods.

3.3.2 Privacy of Reference Points

As pointed out at the end of §3.1, FAPRIL assumes that the set of reference points \( \{\chi_i\}_{i=1}^M \) is made public by the server. While this is the case in related works such as (Nieminen and Järvinen, 2020; Li et al., 2014), in (Järvinen et al., 2019) the reference points were considered “private”. More precisely, PILOT (Järvinen et al., 2019) runs a similar protocol as FAPRIL, but extends the garbled circuit for kNN with an Oblivious Array Access (OAA) circuit, which returns only the k closest coordinates \( \{\chi_i, \ldots, \chi_k\} \). While this seemingly keeps the reference points \( \{\chi_i\}_{i=1}^M \) private, we note that an adversary could simply walk around the building or area and obtain at least most of the coordinates revealing a (almost complete) subset of \( \{\chi_i\}_{i=1}^M \).

One attractive way to prevent the previous attempt is to compute the centroid among the k coordinates also inside the garbled circuit. However, this also reveals information about \( \{\chi_i\}_{i=1}^M \) by triangulation. We omit the detailed description of the possible attacks, but note that it is certainly possible to obtain at least a close replica of \( \{\chi_i\}_{i=1}^M \) in fingerprint-based localization, even if the client only obtains its location coordinate from the server (as it is already the case in the general non-privacy-preserving protocol described in §2.1).

In many real-world scenarios, the reference point pattern could be easily guessed from the building map (e.g., when it is based on individual rooms). The reference point coordinates basically only reveal the strategy for constructing \( \mathcal{D} \), but does not help the adversary to construct a similar database, since the adversary does not have the same equipment for the Received Signal Strength (RSS) measurements. We also note that an attack which tries to build a replica of \( \mathcal{D} \) laboriously, is not an attack against FAPRIL.

To fully hide the used distance metric and all the parameters, one can use Private Function Evaluation (PFE) (Alhassan et al., 2020) which incurs substantial overhead compared to a public distance metric.

4 CORRELATED MULTIPLICATION TRIPLE GENERATION

In this section, we show how to interactively generate Multiplication Triples (MTs) for the special case where one secret shared value is multiplied with several values. More specifically, we want to generate multiplications of the form \( ([a]_{0,i} + [a]_{1,i}) \cdot ([b]_0 + [b]_1) = ([c]_0 + [c]_1) \cdot (\text{mod } 2^b) \) for \( i \in \{1, \ldots, M\} \). As sub-protocol we use a protocol from (Mohassel et al., 2020; Demmler et al., 2015) to multiply a value known in the clear by one party with a vector of values known in the clear by the other party using 1-out-of-2 Correlated Oblivious Transfers (C-OTs). The authors of (Mohassel et al., 2020; Demmler et al., 2015) also considered computing squared Euclidean distances
where the same value is reused, but using the old ABY (Demmler et al., 2015)-style Arithmetic sharing which results for \( N = 241 \) APs and \( M = 505 \) reference points in online communication of 3.7 megabytes whereas we require only 2.5 kilobytes.

4.1 C-OT-based MT generation

We start by giving a short overview of how C-OT (Asharov et al., 2013) is used to generate a single MT as described in (Gilboa, 1999; Demmler et al., 2015). We want to compute a MT consisting of Arithmetic shares \([a_0, a_1, b_0, b_1, c_0, c_1] \in \mathbb{Z}_{2^n}, \ell \in \mathbb{Z}\) such that \((|a_0| + |a_1|) \cdot (|b_0| + |b_1|) = |c_0| + |c_1| \pmod{2^\ell}\) where party \( P_0\) gets to know only its respective shares \([a_i], [b_i], [c_i]\). Multiplying out one sees that the challenge is to securely compute \([|a_0| |b_1|]\) where the shares are held by different parties. (By symmetry, the other cross-term \(|a_1| |b_0|\) can be computed by running the same protocol in parallel in the opposite direction.)

The protocol starts by \( P_0\) randomly generating \([a_0] \in_R \mathbb{Z}_{2^{\ell + q}}\) and \( P_1\) randomly generating \([b_1] \in_R \mathbb{Z}_{2^{\ell + q}}\). Now \( P_0\) and \( P_1\) run several C-OT protocols in parallel. Without loss of generality, we assume that \( P_0\) is the sender and \( P_1\) is the receiver. For each \( j\)-th bit \( B_j\) in \([b_1]\), the parties run a 1-out-of-2 C-OT protocol, where \( P_0\) inputs the correlation function \( f_{\ell} (x) = (|a_0| \cdot 2^j + x) \pmod{2^\ell}\) and obtains \((s_{j,0} r_j, s_{j,1} r_j = |a_0| \cdot 2^j + r_j)\), where \( r_j \in_R \mathbb{Z}_{2^{\ell + q}}\), and \( P_1\) obtains \( s_{j, B_j}\). Now the respective shares are \([|a_0| |b_1]|_0 = \sum_{j=0}^{\ell} (s_{j} r_{j})\) and \([|a_0| |b_1]|_1 = \sum_{j=0}^{\ell} (s_{j} B_{j})\). Correctness and security were shown in (Demmler et al., 2015).

Each 1-out-of-2 C-OT protocol (Asharov et al., 2013) requires \( P_1\) to send \( \kappa\) bits to \( P_0\), who replies with \( \ell\) bits. As we run the protocol twice also for the other cross-term, this yields total setup communication per MT of \(2\ell (\kappa + \ell)\) bits.

4.2 Correlated MT Generation

Now, the goal is to generate an additional MT using the same share \([b_1]\), i.e., Arithmetic shares \([a'_0, a'_1, b_0, b_1, c'_0, c'_1]\) that satisfy \((|a'_0| + |a'_1|) \cdot (|b_0| + |b_1|) = (|c'_0| + |c'_1|) \pmod{2^\ell}\). As observed in (Mohassel et al., 2020), \( P_1\) inputs the same values corresponding to the \([b_1]\) into the C-OT protocols for the first MT and hence the messages from \( P_1\) to \( P_0\) can be reused. Therefore, only the second message from \( P_0\) to \( P_1\) consisting of \( \ell\) bits has to be sent in each C-OT, i.e., an additional \(2\ell\) bits for the second MT. Repeating this construction in parallel \( M\) times yields a total communication of \(2\ell (\kappa + M \cdot \ell)\) bits for \( M\) multiplication triples. An additional optimization described in (Demmler et al., 2015, §III-A5) sends only back those bits of the second C-OT message that are needed for the answer resulting in communication \(2\ell (\kappa + M \cdot (\ell + 1)/2)\) bits. The benefit of this optimization technique depends on the parameters and is further discussed in the full version (van der Beets et al., 2022).

4.3 Application to Matrix Multiplication

The improved correlated MT generation technique described in §4.2 can also be applied to other applications where values re-occur such as matrix multiplication on Arithmetic/Delta shares, which is a very common operation, e.g., in Privacy-Preserving Machine Learning (PPML) (Razavi et al., 2018; Patra et al., 2021). For two matrices \(A^{p \times q}\) and \(B^{q \times r}\), we need to generate \(pqr\) MTs, which requires \(pqr \cdot 2\ell (\kappa + \ell)\) bits of communication in the setup phase using the basic approach of (Demmler et al., 2015). This communication cost was also given in (Patra et al., 2021).

With the optimization, the new computation cost is \(2pqr (\kappa + r)\) bits in the setup phase, which can be reduced even further with the optimization from (Demmler et al., 2015, §III-A5) to \(2pqrl (\kappa + r + 1)/2\) bits.

If we fix \(\kappa = 128\), \(\ell = 32\), \(p, q, r = 100\), one matrix multiplication with the basic approach combined with the optimization (Demmler et al., 2015, §III-A5), i.e., the communication cost is \(2pqr \ell (\kappa + (\ell + 1)/2)\) bits, requires 1.05 terabytes of communication. This is optimized to only 124 gigabytes resulting in factor \(8.6 \times\) improvement in communication.

5 PERFORMANCE EVALUATION

In this section, we benchmark FAPRIL with our implementation using artificial databases of different sizes. We start by inspecting the setup and online phase overheads in §5.1. In §5.2, we inspect the overheads separately for each step of FAPRIL (described in §3.2). In §5.3, we compare our results against the currently best known Privacy-Preserving Indoor Localization (PPIL) schemes of (Järvinen et al., 2019; Nieminen and Järvinen, 2020).

We implemented the client side of FAPRIL on Android smartphones. Our implementation relies on two open source libraries, namely Mobile Private Contact Discovery\(^4\), providing the basis for the Garbled Cir-

\(^4\)https://github.com/contact-discovery/mobile_psi_cpp
cuit (GC) protocol, and \textit{libOTe}$^5$, providing the basis for the Correlated Oblivious Transfer (C-OT) protocol. We develop the Delta sharing protocol based on (Patra et al., 2021). Our full implementation is publicly available under the MIT License$^6$.

We use a Huawei P20 smartphone as our client device and a commodity server as specified in Tab. 1. For our network setup, we simulate a real-world LTE connection as follows: we use simulation scripts on the server side to increase the outgoing latency to 10 milliseconds (ms) and limit the bandwidth to 50 megabits per second (Mbit/s). The smartphone uses a Wi-Fi network to connect to the server, which increases the total Round-Trip Time (RTT) to approximately 16 ms.

<table>
<thead>
<tr>
<th>Table 1: The hardware details of our devices.</th>
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<tbody>
<tr>
<td>CPU Type</td>
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<td>Client</td>
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<td>Server</td>
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For the following experiments, we fix the Received Signal Strength (RSS) quantization to 4 bits, use $k = 3$ for the $k$-Nearest Neighbor Algorithm (kNN), and fix the security parameter $\kappa = 128$. In order to get precise results, we run our experiments 10 times for each case and use the averages.

5.1 Benchmarks

The setup phase communication is shown in Fig. 1. As expected, it grows linearly in the number of Access Points (APs) $N$ and the number of reference points $M$.

The setup run-times grow also linearly. When $N = 50, M = 100$, we only need about 0.28 seconds, but the run-time gets up to 1.48 seconds when we increase $M = 800$. For $N = 250, M = 100$, we have a run-time of 0.59 seconds, which grows to 4.14 seconds for the largest case, namely $N = 250, M = 800$. The online phase is more efficient, and even for our largest setting ($N = 250, M = 800$) we require only 0.20 megabytes of communication and the run-time is 0.15 seconds.

5.2 Detailed Benchmarks

We move to the more detailed view of the overheads. For this, we fix $N = 241, M = 505$ as it represents a real four-story building (see §2.1.2) and collect the results in Tab. 2b. It is clear that the setup phase dominates the total costs for FAPRIL. More precisely, the clear bottleneck is the Multiplication Triple (MT) generation, which requires 7.55 megabytes of communication and a run-time of 2.22 seconds. We note here that our implementation does not take advantage of the optimization of (Demmler et al., 2015, §III-A5) due to integration problems with the \textit{libOTe} library. Therefore, the communication is almost doubled compared to the theoretical case, which is 4.2 megabytes (see §3.2.1). Our implementation also does not take full advantage of parallelization, which could possibly decrease the run-time significantly. FAPRIL can benefit directly from further improvements regarding MT generation, e.g., the recently proposed Silent OT technique (Boyle et al., 2019b; Boyle et al., 2019a) that improves communication at the expense of more computation or MT generation with Ring Learning With Errors (RLWE)-based additively Homomorphic Encryption (HE) (Rathee et al., 2019). We leave implementation of these on mobile phones as future work.

Comparing our concrete communication overheads from Tab. 2b with the complexity analysis, we conclude that our benchmarks are aligned with the theoretical numbers (see §3.2), except for the MT generation (as explained previously) and for Client Garbled Inputs. The reason for the latter is that our implementation takes advantage of the more efficient “Delta-OT” (Burra et al., 2021) as implemented in \textit{libOTe}.

5.3 Performance Comparison to Related Work

In this section, we compare the performance of FAPRIL to the client-server scheme NJ (Nieminen and Järvinen, 2020), and the Arithmetic and Yao sharing (AY) based scheme using squared Euclidean distance from (Järvinen et al., 2019). The results are collected in Tab. 3.

We can see that FAPRIL clearly outperforms
NJ (Nieminen and Järvinen, 2020) except for the setup phase communication, which is expected to be in the favor of NJ even more when the number of APs $N$ increases. On the other hand, we argue that the run-time advantages of FAPRIL makes it more attractive for practical usage. The run-time improvements of $8 \times$ for the setup phase and $27 \times$ for the online phase is significant. We also note that the improvements are expected to be considerably greater for larger settings.

Our comparison to AY (Järvinen et al., 2019) is not completely fair, since it was run in an outsourced setting, where all the computations occur on commodity servers. On the other hand, AY (Järvinen et al., 2019) includes an extra step at the end to obtain the location coordinates using Oblivious Array Access (OA). However, this step could be directly included in FAPRIL (see §3.3.2). Based on their evaluations, the step requires 1.3 megabytes of communication and takes 46 milliseconds. Even with this, FAPRIL achieves similar online run-times and almost $15 \times$ less communication in total compared to AY (Järvinen et al., 2019).

### 6 CONCLUSION AND FUTURE WORK

We presented FAPRIL, a Privacy-Preserving Indoor Localization (PPIL) scheme in the client-server setting based on state-of-the-art Secure Two-Party Computation (STPC). We implemented FAPRIL for Android smartphones and evaluated the performance with various benchmarks representing real world settings. With our optimization technique for generating Multiplication Triples (MTs), we showed that FAPRIL achieves practical run-times and communication. More precisely, for a real world university building setting with 241 Access Points (APs) and 505 reference points, we achieve a online run-time of 96 milliseconds and 129 kilobytes online communication. The setup phase takes 2.5 seconds and requires 9.8 megabytes of communication. With these results, we substantially outperform previously proposed solutions for PPIL.

Lastly, we give a list of interesting topics for future research:

- Analyzing FAPRIL’s power consumption on smartphones.
- Improving the efficiency of the vector-matrix multiplication with secret shares using different MT generation techniques, e.g., Ring Learning With Errors (RLWE)-based additively Homomorphic Encryption (HE) (Rathee et al., 2019).
- Developing protocols that hide the size of the database, the used distance metric, and/or the reference point coordinates from the clients.
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